

Derivation of Eq. (3.7.54) on page 213 is a bit tricky. Use the following definitions in Eq. (3.7.49) with the lower choice of sign:

$$\begin{aligned}
 j_1 &= l \\
 j_2 &= \frac{1}{2} \\
 j &= l + \frac{1}{2} \\
 m_2 &= \frac{1}{2} \\
 m_1 &= n - \frac{1}{2} \\
 m_1 + m_2 &= n \equiv m - 1 \Rightarrow m = n + 1
 \end{aligned}$$

Use only  $n$  rather than  $m$  in evaluation of Eq. (3.7.49). Using the condensed notation in which  $j_1$  and  $j_2$  are suppressed, that equation becomes:

$$\begin{aligned}
 &\sqrt{(l + \frac{1}{2} + [n + 1])(l + \frac{1}{2} - [n + 1] + 1)\langle n - \frac{1}{2}, \frac{1}{2} | l + \frac{1}{2}, n \rangle} \\
 &= \sqrt{(l + n + \frac{1}{2})(l - [n - \frac{1}{2}])\langle n + \frac{1}{2}, \frac{1}{2} | l + \frac{1}{2}, n + 1 \rangle}
 \end{aligned}$$

Replacing  $n$  by  $m$  and combining some terms under the square root, we immediately get Eq. (3.7.54).

$$\begin{aligned}
 &\sqrt{(l + \frac{1}{2} + m + 1)(l + \frac{1}{2} - m)\langle m - \frac{1}{2}, \frac{1}{2} | l + \frac{1}{2}, m \rangle} \\
 &= \sqrt{(l + m + \frac{1}{2})(l - m + \frac{1}{2})\langle m + \frac{1}{2}, \frac{1}{2} | l + \frac{1}{2}, m + 1 \rangle}
 \end{aligned}$$

Also note that you can use Mathematica to compute Clebsch-Gordan coefficients. The notation is `ClebschGordan[{j1, m1}, {j2, m2}, {j, m}]`